

# AMME1362 - Materials

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## Introduction to Materials (Chapter 1)

Material Classification	Properties [chemical bonding, conductivity, application, grain sizes]
<b>Metals</b>	<ul style="list-style-type: none"><li>• Metallic bonding</li><li>• Strong, ductile</li><li>• high thermal &amp; electrical conductivity</li><li>• opaque, reflective.</li></ul>
<b>Polymers/plastics</b>	<ul style="list-style-type: none"><li>• Covalent bonding (sharing of e's)</li><li>• Soft, ductile, low strength, low density</li><li>• thermal &amp; electrical insulators</li><li>• Optically translucent or transparent.</li></ul>
<b>Ceramics</b>	<ul style="list-style-type: none"><li>• ionic bonding (refractory) – compounds of metallic &amp; non-metallic elements (oxides, carbides, nitrides, sulfides)</li><li>• Brittle, glassy, elastic</li><li>• non-conducting (insulators)</li></ul>
<b>Composites</b>	<ul style="list-style-type: none"><li>• Composed of at least 2 different types of materials</li><li>• Produces a new material with enhanced properties such as hardness, tensile strength etc.</li></ul>

### The Materials Selection Process

1. Pick **Application** → Determine required **Properties**

**Properties:** mechanical, electrical, thermal, magnetic, optical, deteriorative.

2. **Properties** → Identify candidate **Material(s)**

**Material:** structure, composition.

3. **Material** → Identify required **Processing/Synthesis**

**Processing:** changes **structure** and **overall shape** ex: casting, sintering, vapor deposition, doping forming (for semiconductors), joining, annealing.

- [changing cooling rate of steel changes hardness, faster cooling greater hardness]
- [adding impurities such as Ni to Copper and deforming Cu increases its resistivity]

PROCESSING/SYNTHESIS -----> MATERIAL -----> PROPERTIES -----> PERFORMANCE/APPLICATION

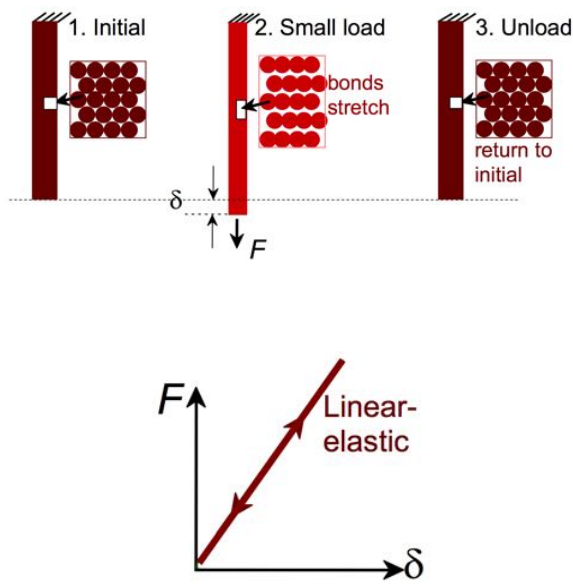
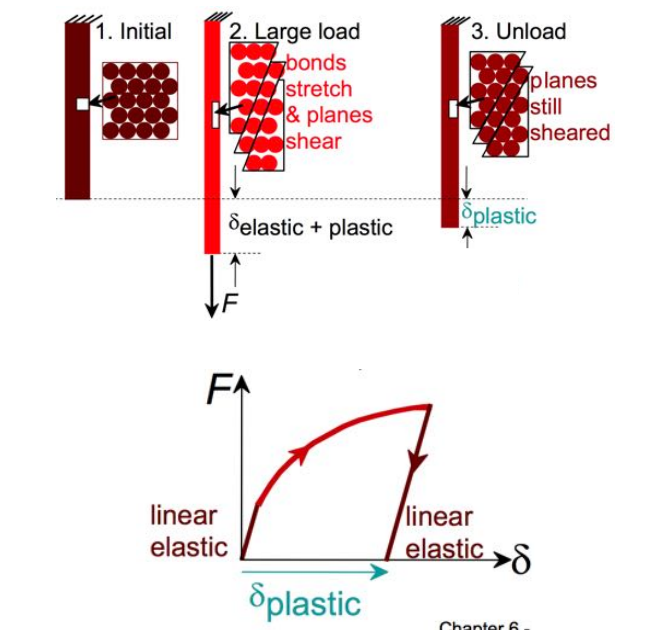
## Mechanical Properties of Metals (Chapter 6)

6.2, 6.4, 6.10, 6.21, 6.30, 6.42, 6.43, 6.60,

KEYWORDS	DEFINITION
Stress & strain	These are size-independent measures of load and displacement, respectively
Elastic behavior	This reversible behavior often shows a linear relation between stress and strain. To minimize deformation, select a material with a large elastic modulus ( $E$ or $G$ ).
Plastic behavior	This permanent deformation behavior occurs when the tensile (or compressive) uniaxial stress reaches $\sigma_y$
Toughness	Energy needed to break a unit volume of material.
Ductility	The plastic strain at failure

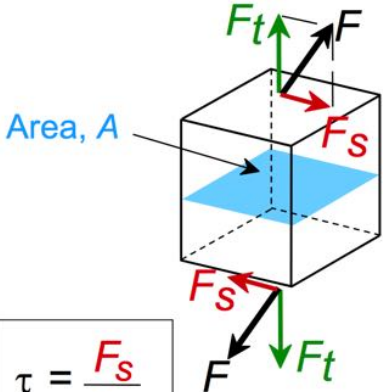
### DEFORMATION

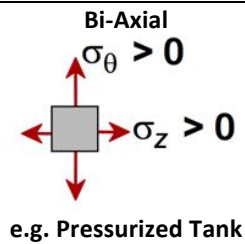
- On an atomic level, elastic deformation of a material corresponds to the stretching of interatomic bonds and corresponding slight atomic displacements.
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Elastic Deformation	Plastic Deformation (METALS)
<ul style="list-style-type: none"> <li>Elastic = reversible</li> <li>Non-permanent (i.e. returns back to its own shape when applied load is released)</li> </ul>	<ul style="list-style-type: none"> <li>Plastic = permanent</li> </ul>
 <p>1. Initial</p> <p>2. Small load</p> <p>bonds stretch</p> <p>3. Unload</p> <p>return to initial</p> <p><math>\delta</math></p> <p><math>F</math></p> <p>Linear-elastic</p>	 <p>1. Initial</p> <p>2. Large load</p> <p>bonds stretch &amp; planes shear</p> <p>3. Unload</p> <p>planes still sheared</p> <p><math>\delta_{\text{elastic}} + \text{plastic}</math></p> <p><math>\delta_{\text{plastic}}</math></p> <p><math>F</math></p> <p>linear elastic</p> <p>linear elastic</p> <p><math>\delta</math></p> <p><math>\delta_{\text{plastic}}</math></p> <p>Chapter 6 -</p> <ol style="list-style-type: none"> <li>A material that is stressed first undergoes elastic, or nonpermanent, deformation.</li> <li>Elastic + Plastic deformation at larger stress</li> <li>Permanent (plastic) after load is removed</li> </ol>

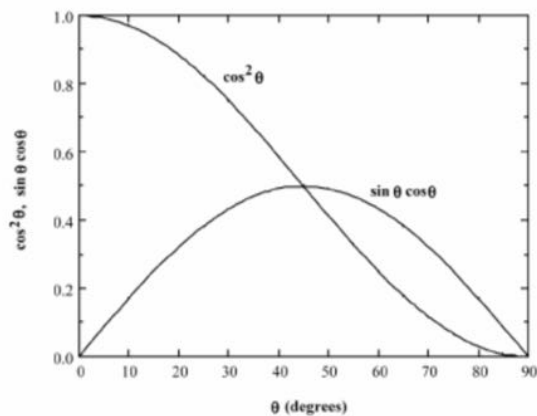
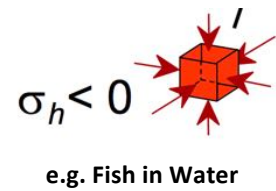
## ENGINEERING STRESS

Engineering stress  $\sigma$  is defined as the instantaneous load divided by the original specimen cross-sectional area

Stress Type	
<p>Tensile (<math>\sigma &gt; 0</math>)</p> <p><b>PERPENDICULAR to Plane</b></p>	 <div data-bbox="833 703 1015 837" style="border: 1px solid black; padding: 5px;"> <math display="block">\tau = \frac{F_s}{A_0}</math> </div> <div data-bbox="1305 591 1481 770" style="border: 1px solid black; padding: 5px;"> <math display="block">\sigma = \frac{F_t}{A_0}</math> <p>original area before loading</p> </div>
<p>Shear (<math>\tau</math>) – scissors</p> <p><b>ON THE PLANE</b></p>	
Compressive ( $\sigma < 0$ )	Torsion [form of shear] – TWIST



Hydrostatic Compression

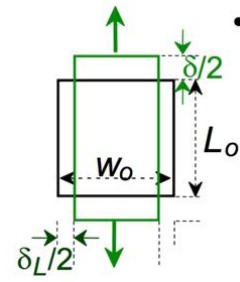
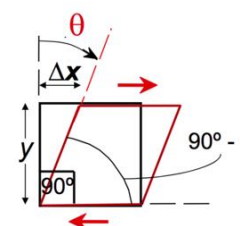


The maximum normal stress at  $\theta = 0^\circ$ .

The maximum shear stress at  $\theta = 45^\circ$

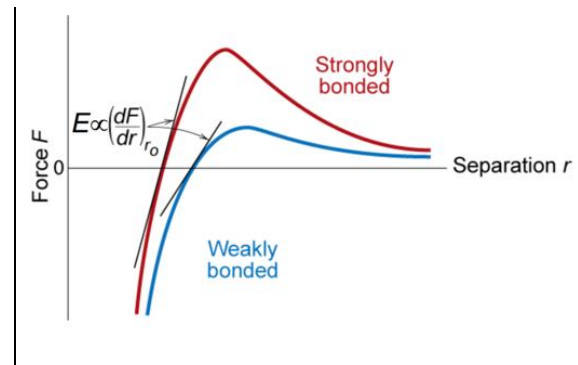
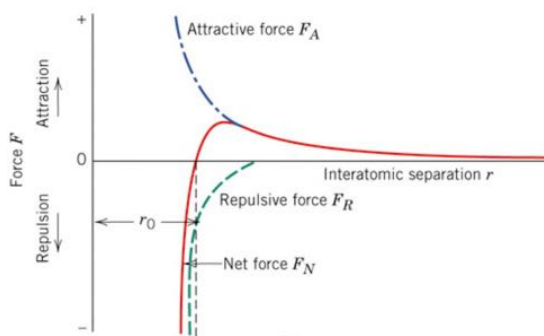
## ENGINEERING STRAIN – NO UNITS/DIMENSIONS

Engineering strain  $\epsilon$  is expressed as the  $\Delta$  in length (in the direction of load application) divided by the original length

<b>Tensile strain</b>	$\epsilon = \frac{\delta}{L_o}$	
<b>Lateral strain</b>	$\epsilon_L = \frac{-\delta_L}{w_o}$	
<b>Shear strain (<math>\gamma</math>)</b>	$\gamma = \frac{\Delta x}{y} = \tan \theta$	

For shear elastic deformations, shear stress ( $\tau$ ) and shear strain ( $\gamma$ ) are proportional to one another. The constant of proportionality is the shear modulus ( $G$ ).

## MECHANICAL PROPERTIES



- **Slope of stress strain plot ( $\propto$  young's elastic modulus)** depends on bond strength of metal
- As atoms get closer, there is greater electrostatic repulsion. There is a point of balance where the net force is zero  $\rightarrow$  the **gradient** determines how strong the bonding between atoms is.

## LINEAR ELASTIC PROPERTIES

- The degree to which a structure deforms or strains depends on the **magnitude of an imposed stress**. For tensile and compressive loading, the slope of the linear elastic region of the stress–strain curve is the **modulus of elasticity (E, stiffness)**, per Hooke's law.
- When most materials are deformed **elastically** [due to reduced load size], stress and strain are proportional— that is, a plot of stress versus strain is linear.

### Hooke's Law:

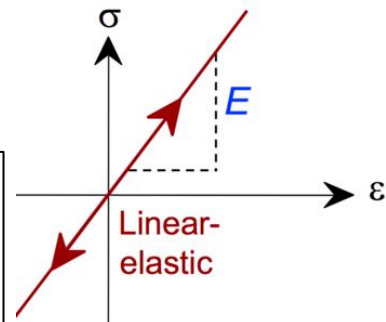
$$\sigma = E \varepsilon$$

Hooke's Law is the relationship between engineering stress and engineering strain for elastic deformation (tension and compression)

E - measure of interatomic bonding force (**GPa or psi**) or stiffness

$\sigma$  - stress placed on material (Nm<sup>-2</sup>)

$\varepsilon$  - epsilon



## ANELASTICITY

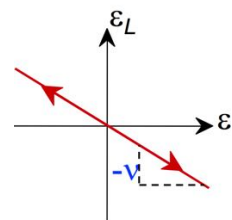
Elastic deformation that is dependent on time is termed *anelastic* [e.g. carbon nanotubes]

## DIFFERENCES BETWEEN PLASTIC, ELASTIC & ANELASTICITY

Plastic deformation is permanent whereas elastic and anelasticity deformation results in the material returning to its original shape completely. However elastic deformation is immediate whereas anelastic deformation takes time

## POISSON'S RATIO

$$\nu \text{ (no units)} = - \frac{\varepsilon_L \text{ (lateral strain - GPa or psi)}}{\varepsilon \text{ (actual strain)}}$$



**NOTE:** If object becomes longer under stress, the width (lateral dimension) will decrease

- $\nu > 0.50$	Density <b>increases</b>
- $\nu < 0.50$	Density <b>decreases</b> → voids form (i.e. widening of the material)

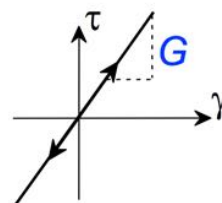
**metals:**  $\nu \sim 0.33$   
**ceramics:**  $\nu \sim 0.25$   
**polymers:**  $\nu \sim 0.40$

## RELATIONSHIP AMONG MODULI AND POISSON RATIO

For shear elastic deformations, shear stress ( $\tau$ ) and shear strain ( $\gamma$ ) are proportional to one another. The constant of proportionality is the shear modulus (G).

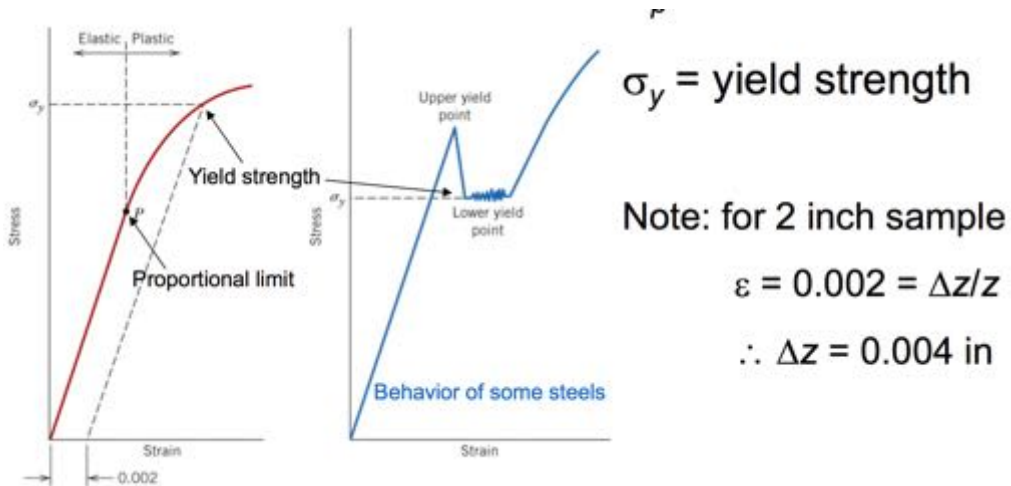
### Elastic Shear modulus, G:

$$\tau = G \gamma$$



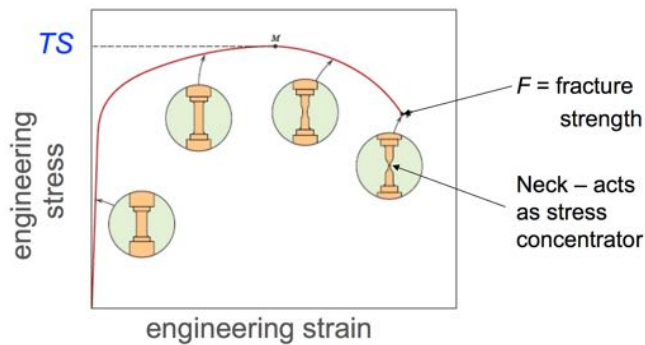
## YIELD STRENGTH, $\sigma_y$

The minimum stress required for plastic deformation of 0.002 (0.2%)



## TENSILE STRENGTH

Maximum stress on engineering stress-strain curve.



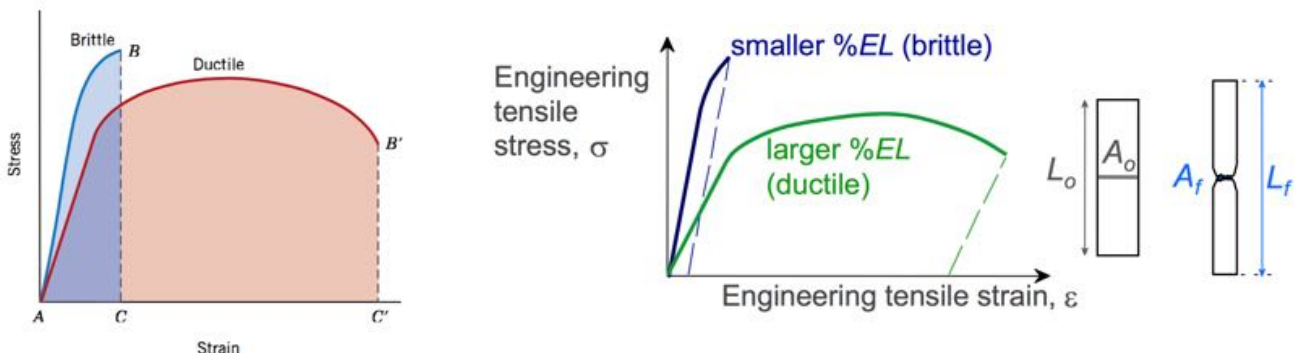
**Metals:** occurs when noticeable **necking** starts.

**Polymers:** occurs when **polymer backbone chains** are aligned and about to break.

## DUCTILITY

Measure of the degree of plastic deformation that has been sustained at fracture. A metal that experiences **very little or no plastic deformation upon fracture** is termed *brittle*

$$\%EL = \frac{L_f - L_o}{L_o} \times 100 \quad \%RA = \frac{A_o - A_f}{A_o} \times 100$$

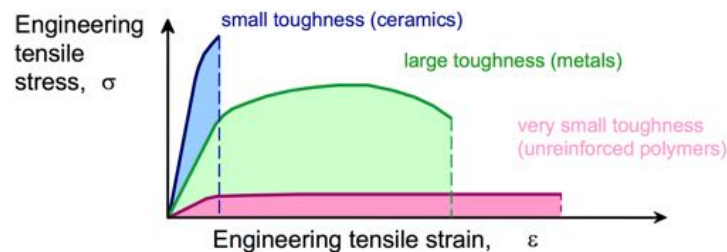


**Brittle fracture:** Elastic Energy

**Ductile fracture:** elastic + plastic energy

## TOUGHNESS (or fracture toughness)

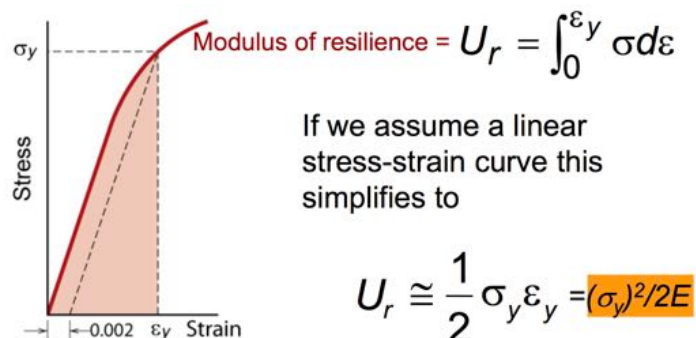
- Energy to break a unit volume of material calculated by area under stress-strain curve
- Measure of material's resistance to fracture when a crack (or other stress-concentrating defect) is present



- The **greater the product of tensile stress and tensile strain**, the greater the toughness
- Metals absorb most amount of energy, hence is used in cars

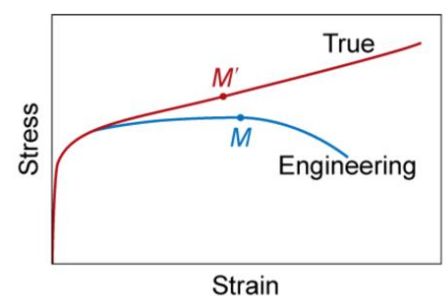
## RESILIENCE, $U_r$

- **Material's ability to store energy for elastic deformation**
- Modulus of resilience – the strain energy per unit volume for stress up to the point of yielding



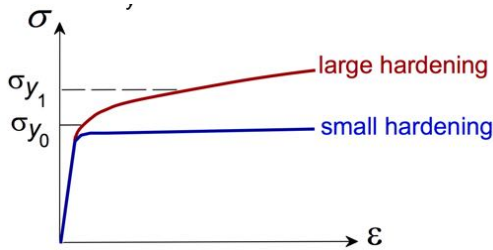
## TRUE STRESS & TRUE STRAIN

- The true stress and true strain are both instantaneous measurements (instantaneous cross-sectional area, length and elongation of length) unlike engineering stress and strain.
- It is a measure taken **BEFORE NECKING** and **ASSUMING THAT THERE IS NO CHANGE IN VOLUME** [i.e.  $A_0 l_0 = A_l l_l$ ]



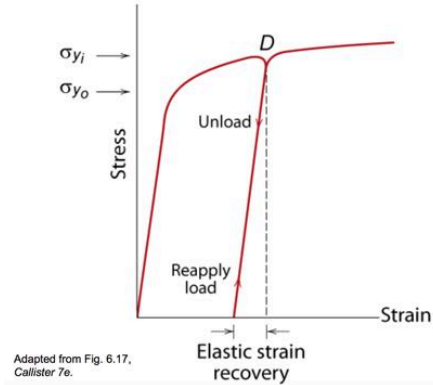
## WORK HARDENING

Work hardening is the **increase in the yield strength** of a material due to plastic deformation [new material has higher yield strength compared to its initial undeformed state]



$$\sigma_T = K(\epsilon_T)^n$$
 strain hardening exponent:  $n = 0.15$  (some steels) to  $n = 0.5$  (some coppers)  
 "true" stress ( $F/A$ )      "true" strain:  $\ln(L/L_0)$

## Work Hardening & Elastic Strain Recovery



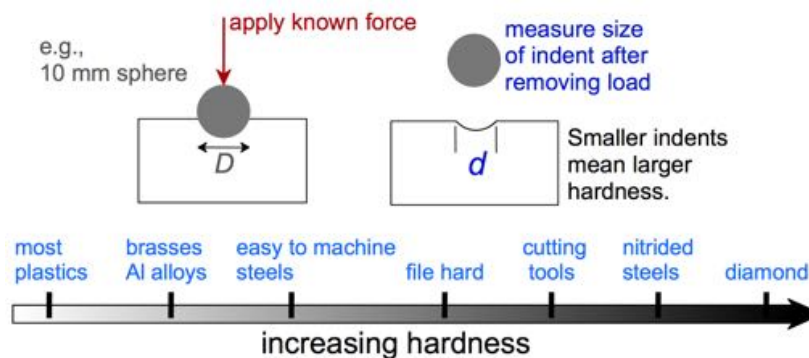
## HARDNESS

Resistance to permanently indenting the surface. Although it is not a well-defined property, it is the property tested most because it is:

- Inexpensive & simple
- Non destructive – causes small indentation
- Able to be approximately converted to other properties (e.g. tensile strength)

Large hardness means:

- resistance to plastic deformation or cracking in compression.
- better wear properties.



- ✓ Smaller Indent = Large Hardness
- ✓ **Hardness is inversely proportional to toughness** (i.e. greater hardness, less toughness)

There are many methods to measure hardness such as:

- Rockwell Method → uses a scale up to 130 (useful only 20-100)
  - Uses a minor (10kg) and major load (A,B,C) to give value
  - If value is <20 or > 100, different major load should be used
  - Hardness Specification 80 HRB → 80 Rockwell hardness on the B scale
- Brinell Test (HB = Brinell Hardness)
- Vickers/Knoll Microhardness

## COMPARISON OF DIFFERENT HARDNESS SCALES:

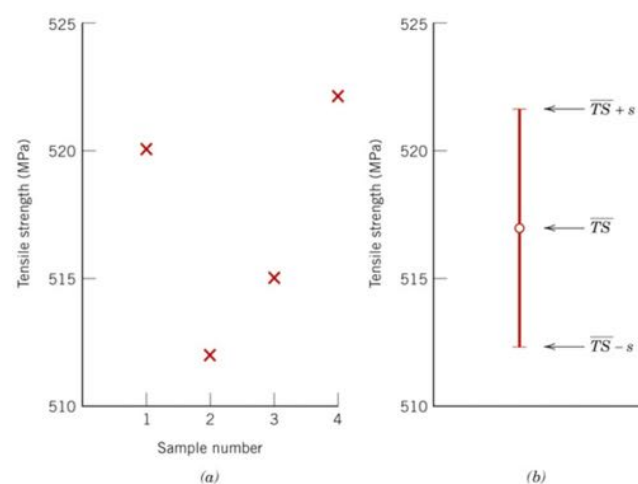
- Comprehensive conversion scheme not available
- Conversion data depend on materials
- Most reliable data exist for steels

## Variability in Material Properties

- Elastic modulus is material property (unique)
- Critical properties depend largely on sample flaws (defects, etc.). Large sample to sample variability.
- Hence we use statistic to acknowledge this variation between specimens

## Scatter in experimental data

- Test method
- Inhomogeneity
- Slight structural difference
- Operator bias



## Structure of Crystalline Solids (Chapter 3)

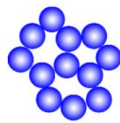
### SUMMARY

1. Materials can be **single crystals** or **polycrystalline**. Material properties generally vary with single crystal orientation (i.e., they are **anisotropic**), but are generally non-directional (i.e., they are **isotropic**) in polycrystals with randomly oriented grains.
2. Some materials can have more than one crystal structure. This is referred to as **polymorphism** (or **allotropy**).
3. **X-ray/electron diffraction** is used for crystal structure and **interplanar spacing** determinations

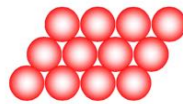
### ENERGY AND PACKING

**Dense, ordered packed structures tend to have lower energies, HENCE more stable.**

Non-Dense Random Packing



Dense Ordered Packing

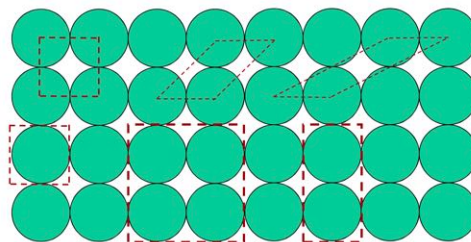


### MATERIAL AND PACKING

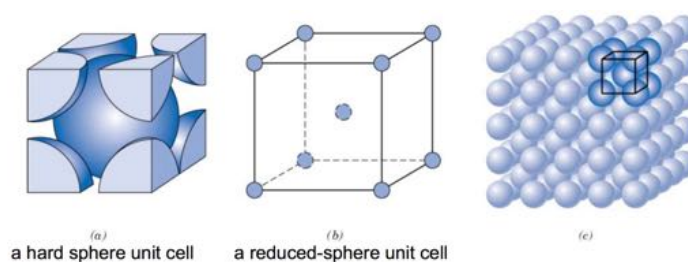
CRYSTALLINE	<ul style="list-style-type: none"><li>➤ atoms pack in periodic 3D arrays</li><li>➤ typical of: all metals, most ceramics, some polymers</li></ul>
NON-CRYSTALLINE = AMORPHOUS	<ul style="list-style-type: none"><li>➤ No periodic packing</li><li>➤ Typical of: complex structures, rapid cooling</li></ul>

### CRYSTAL SYSTEMS (TERMINOLOGY)

**Unit crystal systems:** Smallest repetitive volume with the highest symmetry, which contains the complete lattice pattern of a crystal

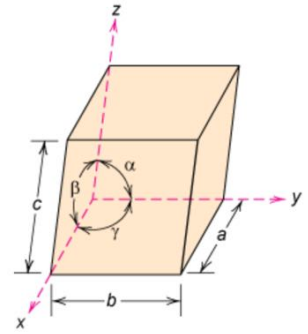


**Atomic hard sphere model,** in which atoms/ions are solid sphere with well-defined diameters, is used to describe crystalline structures



## CRYSTAL PARAMETERS - IMPORTANT

- **Lattice Parameters:**  $a$ ,  $b$ ,  $c$  (edge lengths),  $\alpha$ ,  $\beta$ , and  $\gamma$  (inter-axial angles)
- **Coordination Number** – no. of nearest neighbour/touching atoms
- **Atomic Packing Factor** ( $APF = \frac{\text{Volume of atoms in unit cell}}{\text{Total Unit Cell Volume}}$ )



## METALLIC CRYSTAL STRUCTURES

1. **Tend to be densely packed because --**
  - a. Usually one element is present, so all atomic radii are the same.
  - b. Metallic bonding is not directional → **allows atoms to be closely packed**
  - c. Nearest neighbor distances tend to be small in order to lower bond energy
  - d. Electron cloud shields cores from each other
2. **Have the simplest crystal structures.**

### The 4 main structures of metallic crystals are:

<p><b>Simple cubic</b></p> <p>SC</p>	<ul style="list-style-type: none"> <li>• Rare due to low packing density (only Po has this structure)</li> <li>• <b>Close-packed directions</b> are cube edges.</li> </ul> <p><b>No. of atoms in unit cell:</b> 1 <b>Coordinate No:</b> 6</p>	<p>close-packed directions</p> <p>atoms unit cell: 1 volume atom: <math>\frac{4}{3}\pi(0.5a)^3</math> APF = <math>\frac{1 \cdot \frac{4}{3}\pi(0.5a)^3}{a^3}</math> volume unit cell: <math>a^3</math></p>
<p><b>Body-centered cubic (BCC)</b></p> <p>BCC</p>	<ul style="list-style-type: none"> <li>• Atoms touch each other along <b>cube diagonals</b></li> <li>• ex: Cr, W, Fe (<math>\alpha</math>), Mo</li> </ul> <p><b>No. of atoms in unit cell:</b> 2 <b>Coordinate No:</b> 8</p>	<p><math>\sqrt{3}a</math> <math>a</math> <math>\sqrt{2}a</math></p>
<p><b>Face-centered cubic (FCC)</b></p> <p>FCC</p>	<ul style="list-style-type: none"> <li>• Atoms touch each other along <b>face diagonals</b>.</li> <li>• Stacking Sequence = ABCABC..</li> <li>• ex: Al, Cu, Au, Pb, Ni, Pt, Ag</li> </ul> <p><b>No. of atoms in unit cell:</b> 4 <b>Coordinate No:</b> 12</p>	<p><math>\sqrt{2}a</math> <math>a</math></p>