

# CASH FLOWS, NPV AND COST OF CAPITAL OF A PROJECT

## DETERMINE WHEN TO START AN INVESTMENT

### INVESTMENT TIMING

- If the timing decision does not affect other future decisions that you might wish to make, you should choose the timing with the highest NPV
- You maximise the NPV of your investment if you commence the project as soon as the rate of increase in value drops below the cost of capital

## CHOOSE BETWEEN PROJECTS WITH DIFFERENT LIVES USING EQUIVALENT ANNUAL CASH FLOWS (EAC)

- For mutually exclusive projects, we should compare the assets on their equivalent annual cash flow (EAC) if the choice made today will affect future decisions

### LONG VS SHORT LIVED EQUIPMENT

- This is simply finding the PMT of an ordinary annuity where you use the NPV as the PV

$$Pmt = \frac{NPV}{[(1 - [1 + i]^{-n})/i]}$$

## PROJECT REPLACEMENT DECISION

### CRITICAL ASSUMPTIONS OF ANNUITY/PERPETUITY

$$PV = PMT \frac{1 - (1+i)^{-n}}{i} \text{ or } PV = \frac{PMT}{i}$$



1. The first annuity payment is at the end of the first period
  2. There are **n** payments in the annuity series or infinite number of payments in the perpetuity
  3. PV is calculated at year 0
- If the first annuity payment is at the end of year 2 and there are 9 payments in the series, the PV calculated as at year 0:

A horizontal timeline starting at 0 and ending at 10. Above the timeline, 'PMT' is written above each tick mark from 2 to 10. The tick marks are labeled 0, 1, 2, 3, ..., 9, 10.

$$PV = PMT \left[ \frac{1 - (1+i)^{-9}}{i} \right] (1+i)^{-1}$$

- If the first payment is at the end of year 2 and there are infinite number of payments in the series, the PV calculated as at year 0:

A horizontal timeline starting at 0 and ending at infinity. Above the timeline, 'PMT' is written above each tick mark from 2 to infinity. The tick marks are labeled 0, 1, 2, 3, ..., infinity.

$$PV = \left[ \frac{PMT}{i} \right] (1+i)^{-2}$$

## DEFINE PROJECT COST OF CAPITAL

### WHY DO WE NEED A COST OF CAPITAL?

- The cost of capital is used to discount the expected cash flows of a project to their present values:

$$PV = \sum_{t=1}^n \frac{C_t}{(1+r)^t}$$

- The cost of capital,  $r$ , is also referred to as the discount rate, hurdle rate, required rate of return or opportunity cost of capital

### PROJECT COST OF CAPITAL

- In principle, each project should be evaluated at its own opportunity cost of capital which depends on project risk, not on the company undertaking the project
- The opportunity cost of capital is the expected return that is forgone by investing in a project rather than in financial securities with the same risk
- If the project is high-risk, a firm should use a higher cost of capital than if the project is low-risk
- The CAPM/ SML is used to estimate the project cost of capital if a firm can figure out the project beta (asset beta) that reflects the project risk:

$$r_{\text{project}} = r_f + \beta_{\text{project}} (r_m - r_f)$$

- Project betas are not available in most cases, so most companies start with the company cost of capital as a benchmark discount rate for new investments

## SHOW WHEN TO USE COMPANY COST OF CAPITAL

### COMPANY COST OF CAPITAL

- Is the opportunity cost of capital for investment in the firm as a whole
- Is defined as the expected return on a portfolio of the firm's existing debt and equity securities
- Is usually calculated as a weighted average cost of capital:

$$\text{Company cost of capital} = r_{\text{assets}} = \frac{D}{D+E} r_{\text{debt}} + \frac{E}{D+E} r_{\text{equity}}$$

- It is a useful starting point for setting discount rates for safer or riskier projects
- It is easier to add to, or subtract from, the company cost of capital than to estimate each project's cost of capital from scratch
- Many firms, however, use the company cost of capital to discount the forecasted cash flows on all new projects and this results in good low-risk projects with truly positive NPVs being rejected and poor high-risk projects accepted

### DEBT AND THE COMPANY COST OF CAPITAL

- If no debt is outstanding, the company cost of capital is just the cost of equity  $r_{\text{equity}}$
- With debt and company taxes existing, the company cost of capital is typically called the weighted-average cost of capital or WACC:

$$\text{WACC} = r_{\text{debt}} (1-T) \frac{D}{D+E} + \frac{E}{D+E} r_{\text{equity}}$$

- $r_{\text{debt}}(1 - T)$  reflects interest being a tax-deductible expense