

1. Descriptive statistics

Terminology

Population – the set of all possible measurements of interest

Sample – a subset of measurements from the population

Graphs and tables

Stem and leaf plots

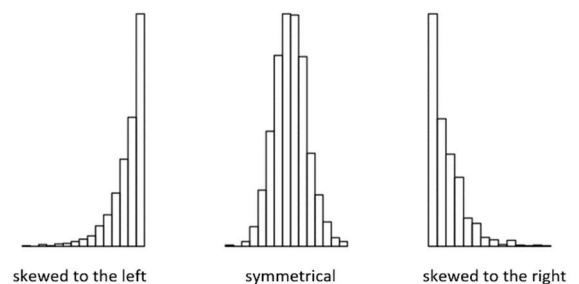
- Don't summarise – present all available info → used for small data sets
- Data split into stem and leaf components → *shape* of distribution
 - Stem
 - Leaf – only final digit of observation
- By default, vertical line = decimal point

Frequency distribution

- Summarise → used for large data sets
 - Intervals/bins
 - Should have same length
- $$\text{length of bin} = \frac{\text{range of data}}{\text{number of bins}} \quad (\text{round to next integer})$$
- Will be right-closed i.e. observation on the boundary between 2 bins will be included in the left bin e.g. (8, 10]
 - Cumulative frequency – total frequency up to and including a particular class
 - $\text{relative frequency} = \frac{\text{frequency}}{\text{sample size}}$

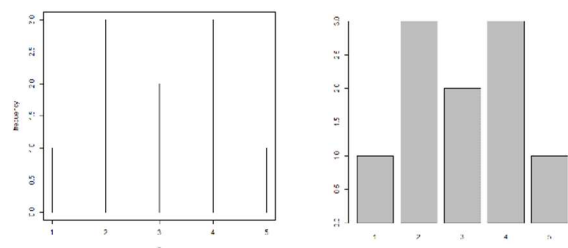
Histogram

- Represents frequency distribution graphically
- For continuous data
- Describe main features of data
 - Overall pattern
 - Area of conc.
 - Presence/absence of outliers
 - *Shape* of distribution
 - Skewed to the left – left side stretches further from peak than right side
 - Symmetric – opposing sides approx.. symmetric about the middle
 - Skewed to the right – right side stretches further from peak than left side



Ordinate diagram or barplot

- For discrete data
- Plot of f_x against x



Measures of location

- Attempt to provide a single numerical value which represents whole data set

Mean = \bar{x} – the simple average

- + Simple to calculate
- Can be greatly affected by extreme observations – pulled towards them
- Inappropriate when working with skewed distributions

$$\frac{1}{n} \sum_{i=1}^n x_i$$

Median = \tilde{x} – the middle value

- If number of observations is even – \tilde{x} = average of middle 2 observations
- + Not affected by outliers

Mode – the value that appears most frequently

- + Relevant for categorical and numerical data
- Might not exist
- Might not be unique – possible to have a bimodal distribution (2 modes)

Shape of distribution

- Mean = median = mode → symmetric
- Mean > median > mode → skewed to the right
- Mean < median < mode → skewed to the left

Measures of spread or dispersion

Variance = s^2 – a measure of the spread around \bar{x}

- In terms of squared distances between the observations and \bar{x}
- In units²
- Dividing by $(n - 1)$ → unbiased population variance
- Always non-negative
- Variance = 0 if and only if all observations are equal to each other
- Large values of s^2 → more spread around \bar{x} = highly volatile
- Small values of s^2 → more conc. around \bar{x} = less volatile
- *deviation of the observation = sample mean – observation*

$$\frac{1}{n-1} \left[\sum_{i=1}^n x_i^2 - \frac{1}{n} \left(\sum_{i=1}^n x_i \right)^2 \right]$$

Standard deviation = s

- Same units as data

$$s = \sqrt{\text{variance}} = \sqrt{s^2}$$