## Contents

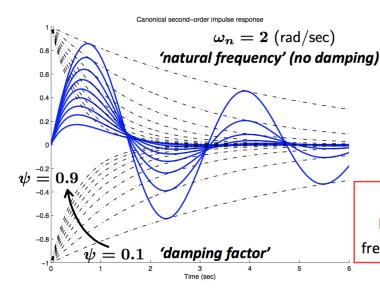
| 1  | ${\rm Linearization}(2013~{\rm Q1},~2012~{\rm Q2})$                                     | 2         |
|----|---|-----------|
| 2  | Pole-zero plot $(2013 \text{ Q2}, 2012 \text{ Q4})$                                     | 3         |
| 3  | Routh Array(2013 Q2, 2012 Q4)   | 5         |
| 4  | Gain margin and Phase $\mathrm{margin}(2013~\mathrm{Q2}~\mathrm{Q4},~2012~\mathrm{Q1})$ | 6         |
| 5  | Closed-loop block diagram and sensitivity functions (2013 Q3 Q4, 2012 Q1 Q3)            | 7         |
| 6  | Frequency response and bode plot  | 7         |
| 7  | Phase-lag and phase-lead control (2013 Q3, 2012 Q1)                                     | 9         |
| 8  | Pole placement (2013 Q3, 2012 Q3)   | 11        |
| 9  | Nyquist plot (2013 Q3, 2012 Q2 Q4)  | <b>12</b> |
| 10 | Root locus (2013 Q4, 2012 Q1 Q2)  | 13        |
| 11 | Time-domain characteristics (2013 Q4, 2012 Q1)  | 14        |

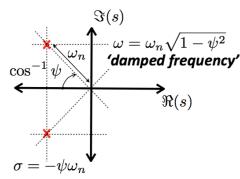
## 2 Pole-zero plot(2013 Q2, 2012 Q4)

• Pole plot and the correspond time domain step response

$$\ddot{y}(t) + 2\psi\omega_n\dot{y}(t) + \omega_n^2y(t) = \omega_n^2u(t) \quad \stackrel{\mathcal{L}}{\leftrightarrow} \quad G(s) = \frac{Y(s)}{U(s)} = \frac{\omega_n^2}{s^2 + 2\psi\omega_n s + \omega_n^2}$$

for 
$$0<\psi<1$$
 the poles are  $\dfrac{-2\psi\omega_n\pm\sqrt{(2\psi\omega_n)^2-4\omega_n^2}}{2}=-\psi\omega_n\pm j\omega_n\sqrt{1-\psi^2}$ 

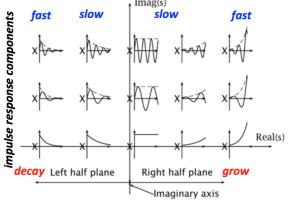




time-constant inc. as damping dec.

peak of oscillation inc. as damping dec.

frequency of oscillation inc. as damping dec.



- response due to poles with +ve real part grows and these are said to be 'unstable'
- response due to poles with -ve real part decays and these are said to be 'stable'
- response due to imaginary axis poles is bounded if not repeated, else response grows
- a stable response is dominated by 'slowest' poles (i.e. closest to imaginary axis)